



Lecture 2A



Phase Diagrams and Microstructures

Monday 9th November 2020

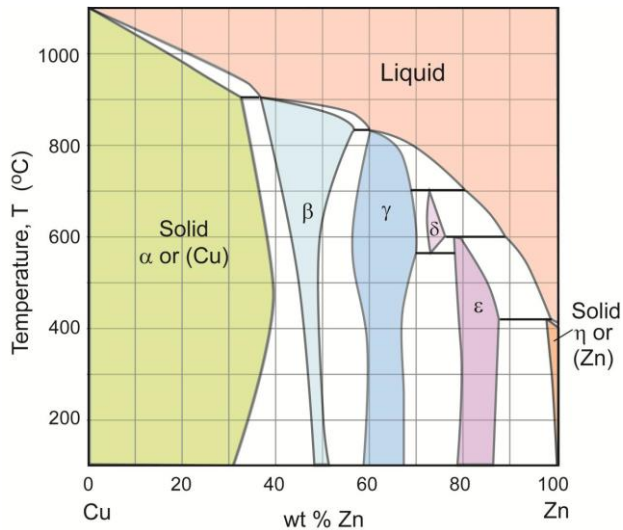
Why do phases matter to manufacture?

Metals are melted and solidified during *casting* and *welding*, but also during *atomization* (metal powder making) and *powder bed fusion AM* by *laser* or *electron beam*



Equilibrium ***phase diagrams*** are one step towards understanding metal microstructures and properties after melting or heat treatments. ***Phase transformations*** another.

Learning Outcomes



- Knowledge of microstructures and phases of binary alloys.
- Understanding of how to interpret phase diagram information.
- Ability to apply phase diagrams to define microstructures.

Study guide for lecture 2A

Minimum reading:

- Lecture slides 2A
- Teach yourself Phase Diagrams and Phase Transformations, part 1-3 and exercises within

Supplementary recommended resources:

- Phase diagram tool within GRANTA EduPack MS&E database
- Ashby Ch 3-4 (just up until and including iron-carbon)
- Callister (any edition): Chapter on Phase Diagrams
- For advanced understanding of calculations, some YouTube links

<https://www.youtube.com/watch?v=h5dwpTqacqc>

<https://www.youtube.com/watch?v=AbXliN8iAeU>

<https://www.youtube.com/watch?v=IUMcbctDNtM>

Recommended extra exercises:

Micro-projects 2A-B

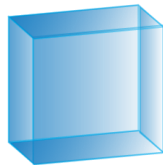
Outline

- Introduction to Phase Diagrams
- Microstructures and binary alloys
- Isomorphous binary phase diagrams
- Eutectic binary phase diagrams
- Lever rule for phase fractions
- Iron – Carbon Phase Diagram and the Granta EduPack software tool

What is a phase?

DEF: A *phase* is a homogeneous portion of a (material) system that has uniform physical and chemical characteristics

Solid phase: ice



Liquid phase: water

Gas phase: water vapor



Classic example: Water

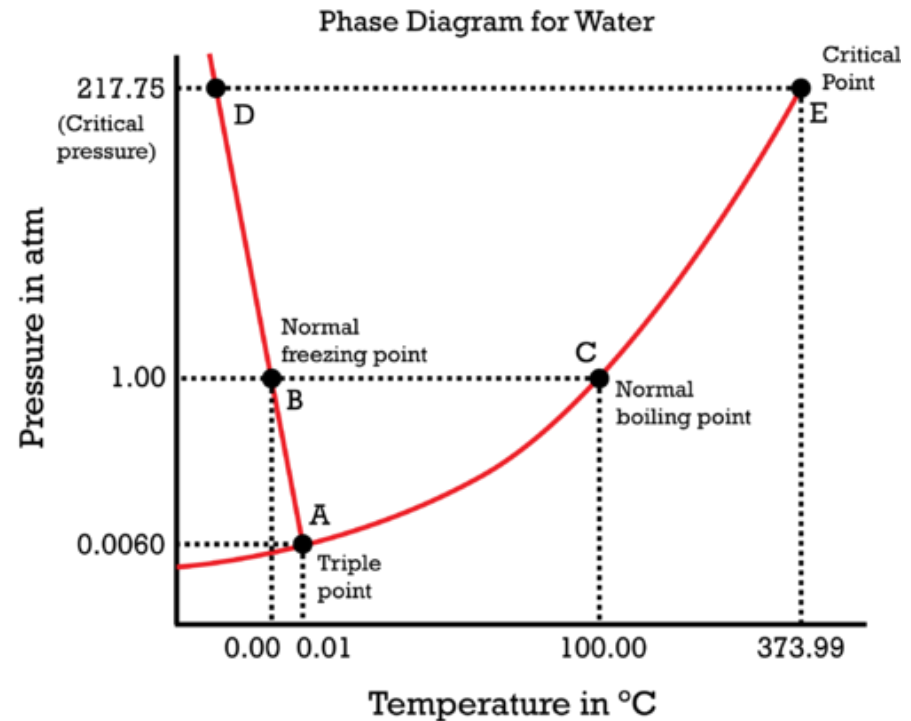
Metals are normally in the solid phase at room temperature but can be melted and even vaporized at high temperatures

Phase Diagrams help us understand materials

DEF: *Phase Diagrams* graphically show information about the **equilibrium** phase structure of a material system with respect to temperature, pressure, and composition

Single component phase diagrams
show temperature and pressure

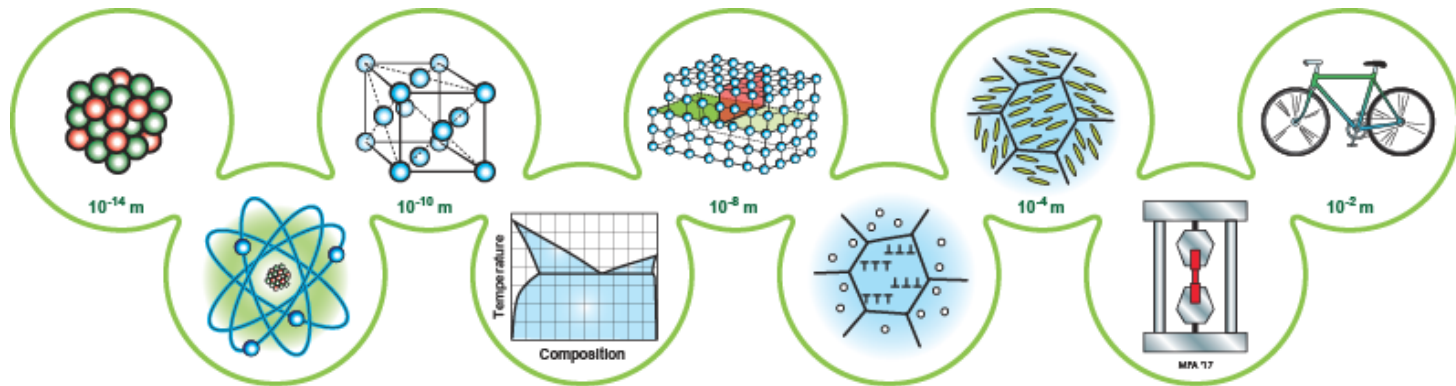
One composition → held constant



<https://courses.lumenlearning.com/cheminter/chapter/phase-diagram-for-water/>

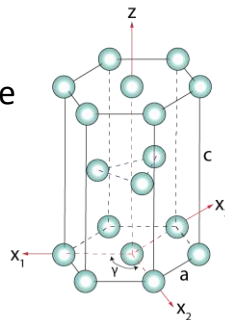
For metals it is more than just liquid, solid, and gas!

DEF: All parts of an alloy **microstructure** with the same atomic structure are a *single phase*



Alpha Titanium

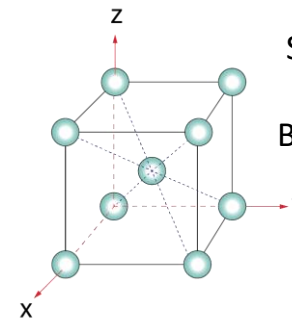
Stable below 882°C
HCP Crystal Structure



882°C

Beta Titanium

Stable between 882-
1670°C
BCC Crystal Structure



What is a binary metal alloy?

DEF: A *metallic alloy* is a mixture of a metal with other metals or non-metals.

1 H																	2 He	
3 Li	4 Be																	10 Ne
11 Na	12 Mg																	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
55 Cs	56 Ba	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu		
87 Fr	88 Ra	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr		



DEF: The *components* are the chemical elements that make up alloys (here, atoms)

DEF: A *binary alloy* contains two components. A *ternary alloy* contains three, etc.

Binary Phase Diagrams

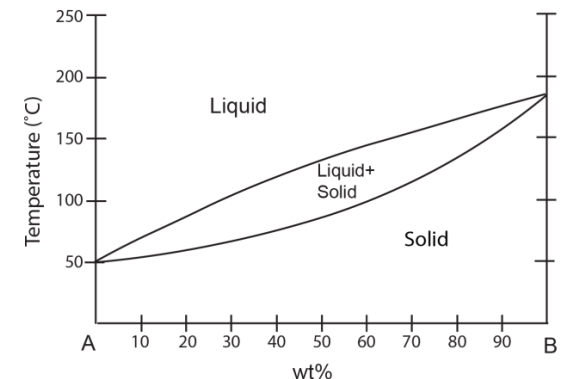
DEF: The *constitution* of an alloy is described by:

- (a) the phases present;
- (b) the weight fraction of each phase;
- (c) the composition of each phase.

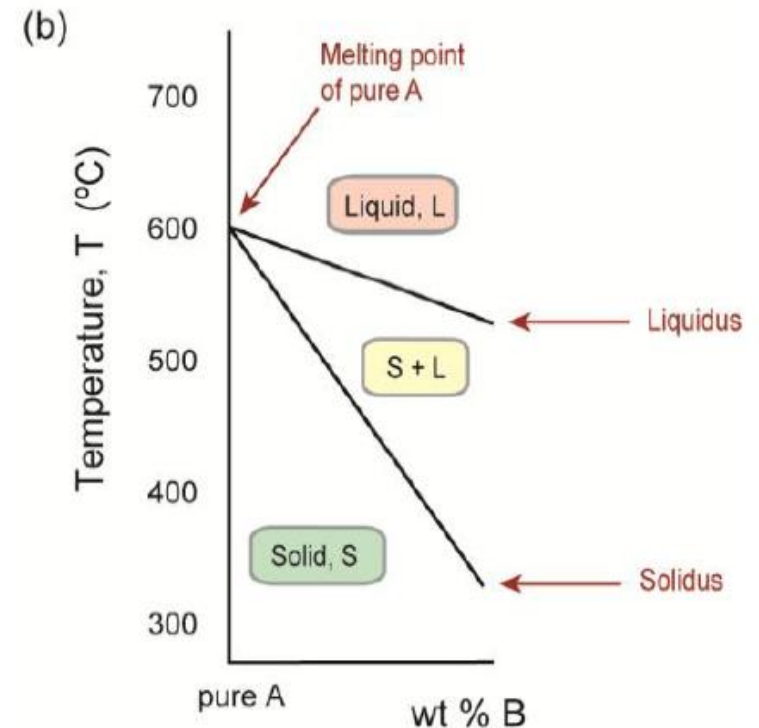
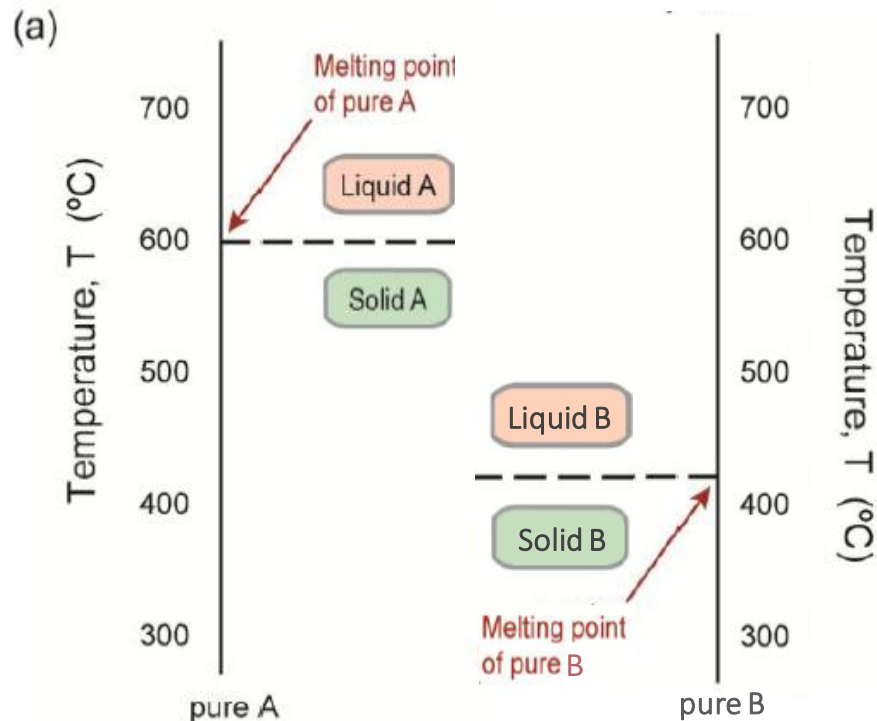
DEF: The *equilibrium constitution* is the state of lowest Gibbs free energy G , for a given composition, temperature and pressure. An alloy in this state shows no tendency to change – it is thermodynamically stable.

DEF: A binary *phase diagram* (or equilibrium diagram) is a diagram with T and composition as axes, showing the equilibrium constitution.

- Graphical representation of the phases present for a two-component system
- Two axis are temperature (y-axis) and composition (x-axis)
- Third variable pressure, is assumed to be one atmosphere
- Most common in materials engineering

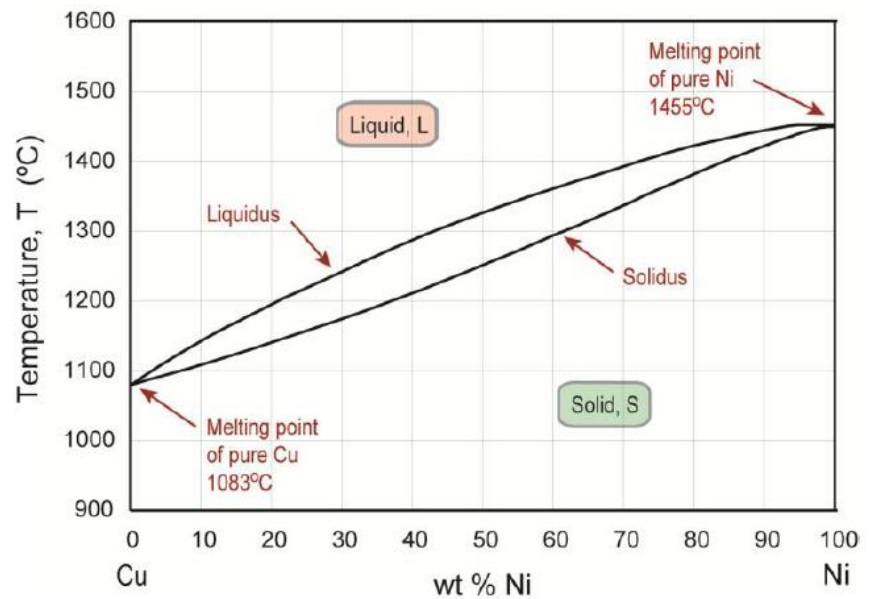


Mixing two metals with different melting point

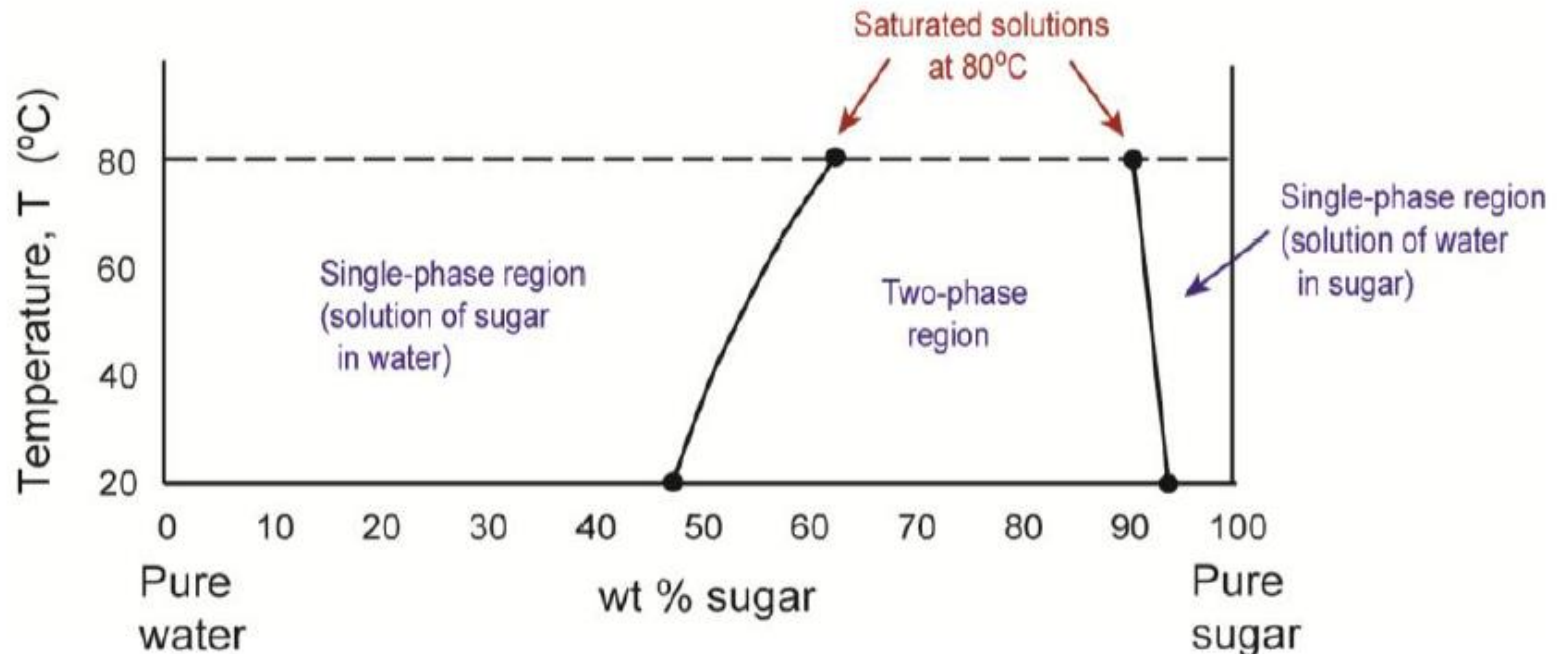


Binary Isomorphous Phase Diagrams

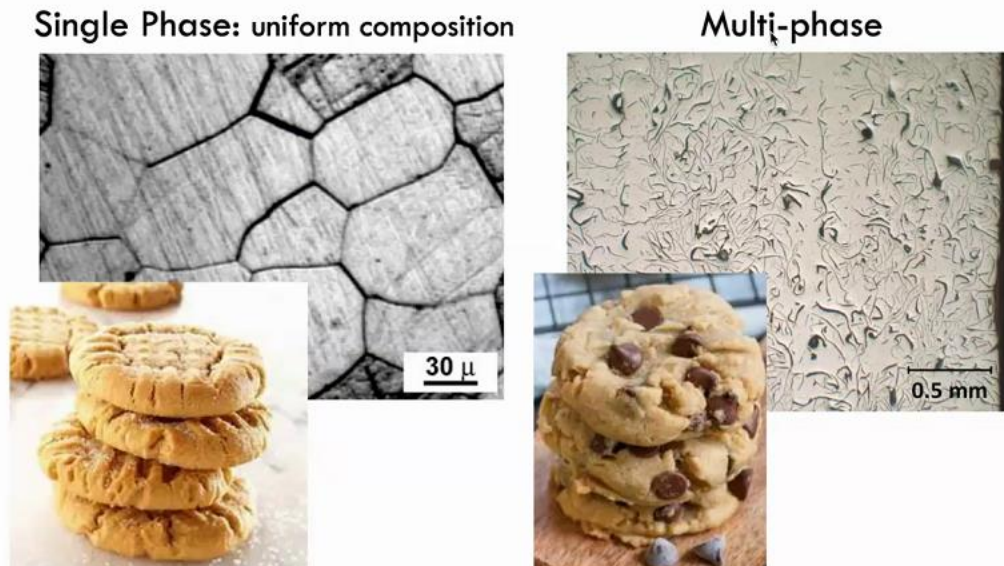
- Complete liquid and solid solubility
- Only one liquid and solid phase across the complete composition range
- Often due to similar atomic crystal structures of the two components
- E.g. Copper and Nickel



Incomplete solubility of components – sweet tea



Single and two-phase solid systems

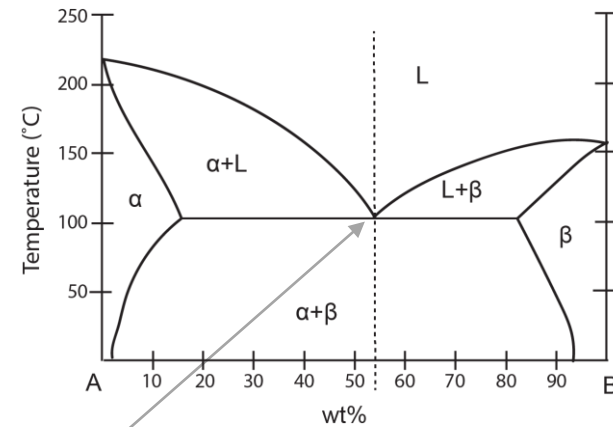


Images from: Dr Amber Genau, University of Alabama, Birmingham

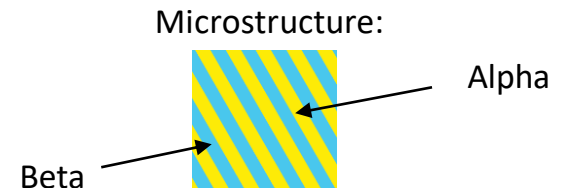
Binary Eutectic Phase Diagram

DEF: The lower limit of the single-phase liquid field formed by the intersection of two liquidus lines is called the *eutectic point*.

- Incomplete solubility within the solid phases
- Leads to a *eutectic reaction* at a specific composition and temperature
- Where the liquid solidifies into two unique solids, alpha and beta



Reaction:
 $L \leftrightarrow \alpha + \beta$



Microstructures and Phase Diagrams

Phase Diagrams

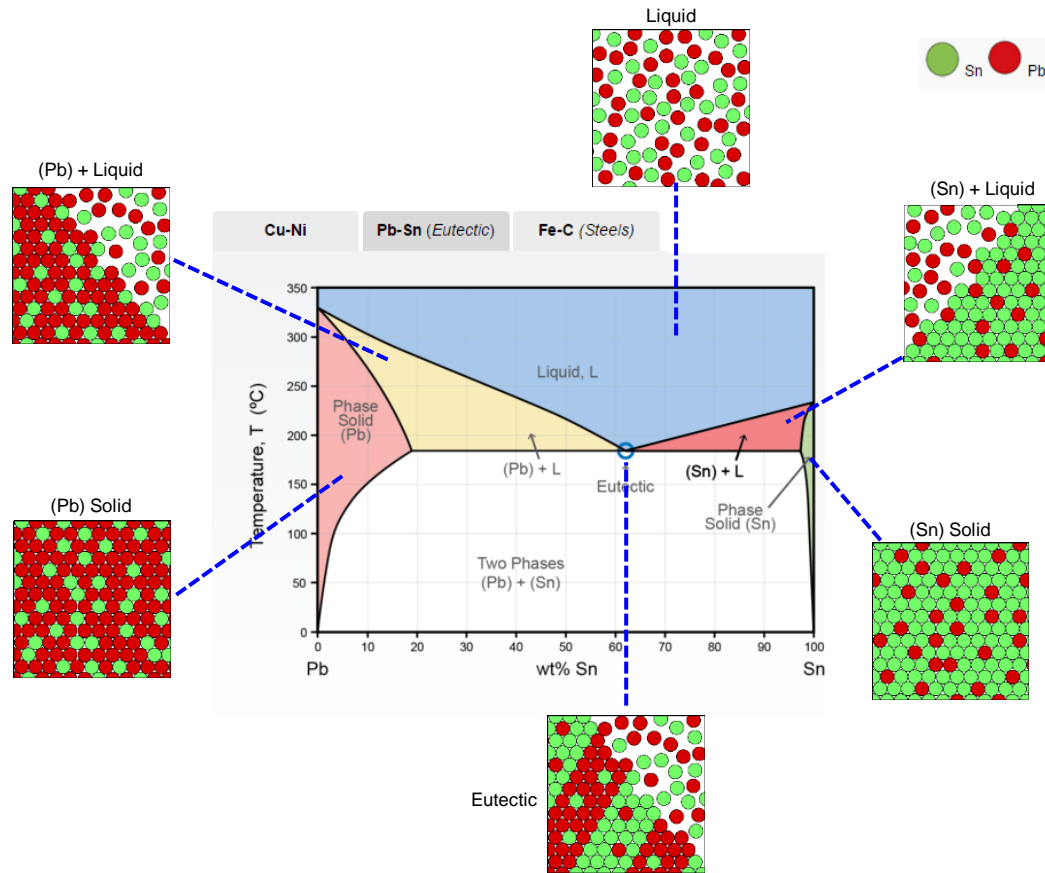
[Phase Diagram glossary](#)

[Lever Rule](#)

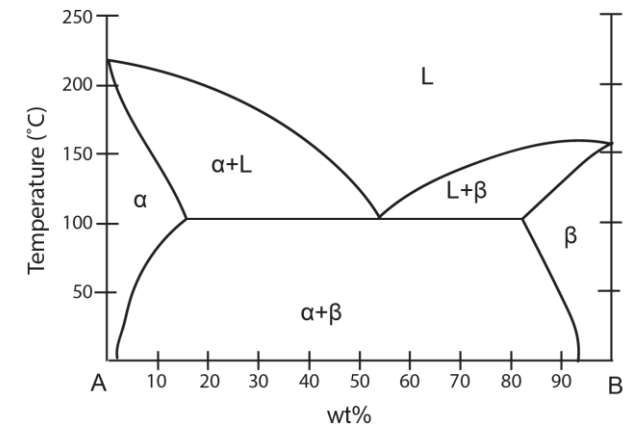
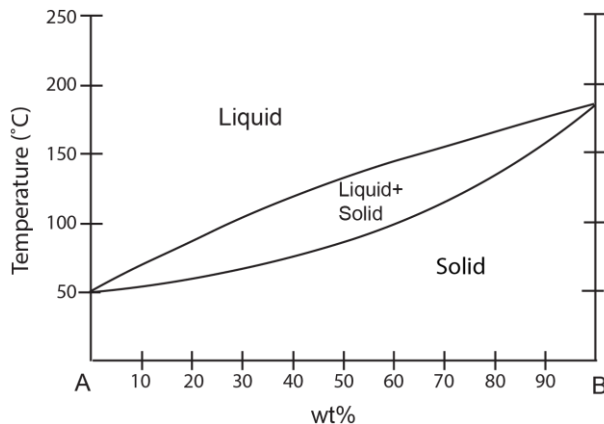
[Phases](#)

[Cooling paths](#)

[Phase diagram datatable](#)



Key Phase Diagram Terminology

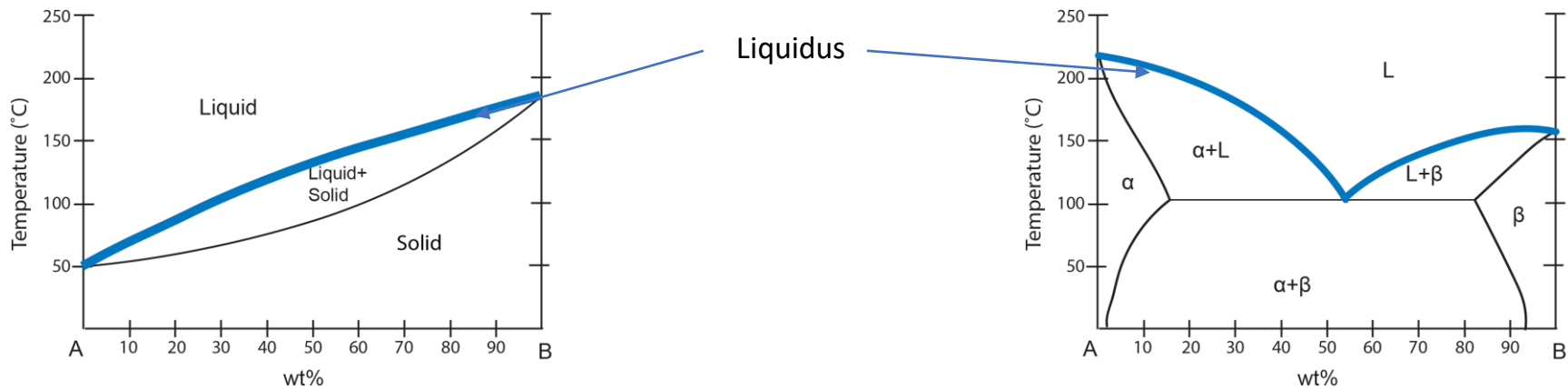


DEF: The *constitution* of an alloy is described by:

- (a) the phases (α , β) present;
- (b) the weight fraction of each phase;
- (c) the composition of each phase.

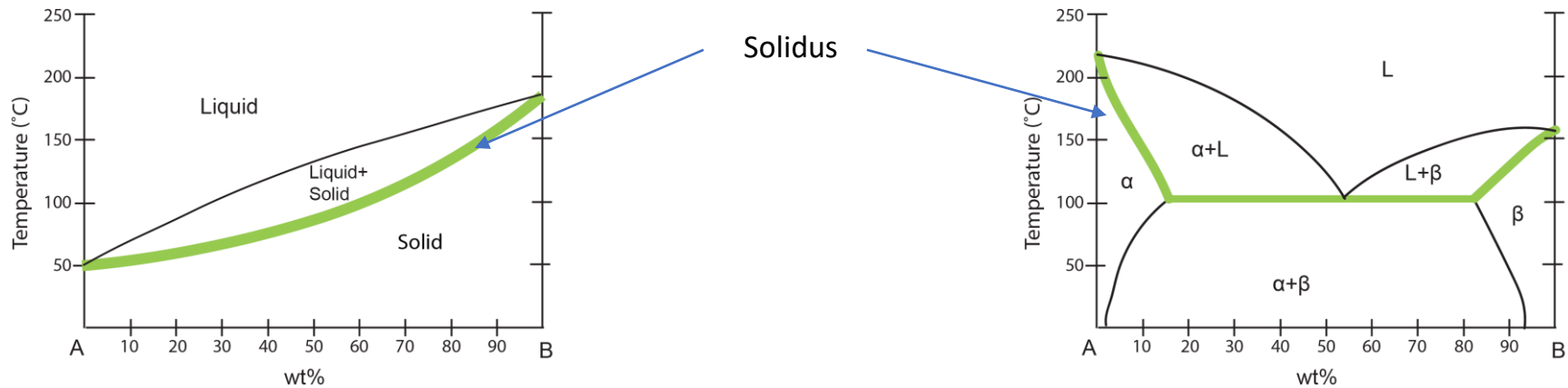
DEF: The lower limit of the single-phase liquid field formed by the intersection of two liquidus lines is called the *eutectic point*.

Key Phase Diagram Terminology



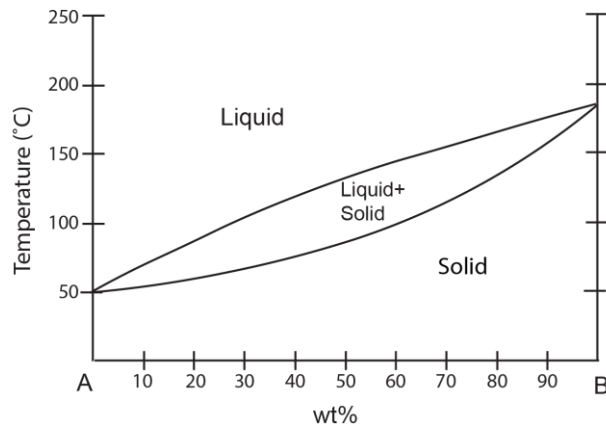
DEF: The phase boundary which limits the bottom of the *liquid* field is called the *liquidus line*.

Key Phase Diagram Terminology

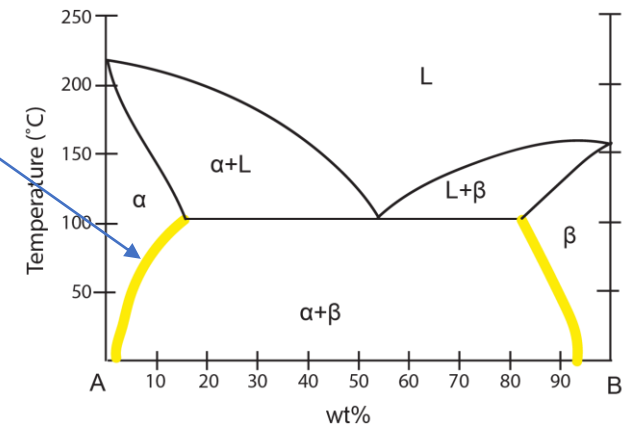


DEF: The line giving the upper limit of the single phase *solid* field is called the *solidus line*.

Key Phase Diagram Terminology



Solvus

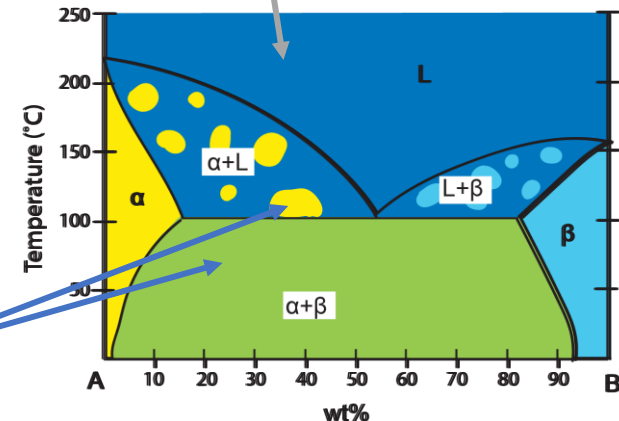


Phase Fractions within Systems

Understanding what phases will be found at specific composition and temperature is incredibly important for alloy development

In two-phase regions, the Lever Rule is needed to calculate the phase fractions

In a single-phase regions, identifying phase fractions is simple



DEF: In a single-phase region, phase and alloy compositions coincide. In a two-phase region the phase compositions lie on the phase boundaries at either end of a horizontal tie-line through the constitution point.

What can the Lever Rule Determine?

Weight fraction of single phases

Liquid, alpha, beta, etc.

Weight fraction of microconstituents

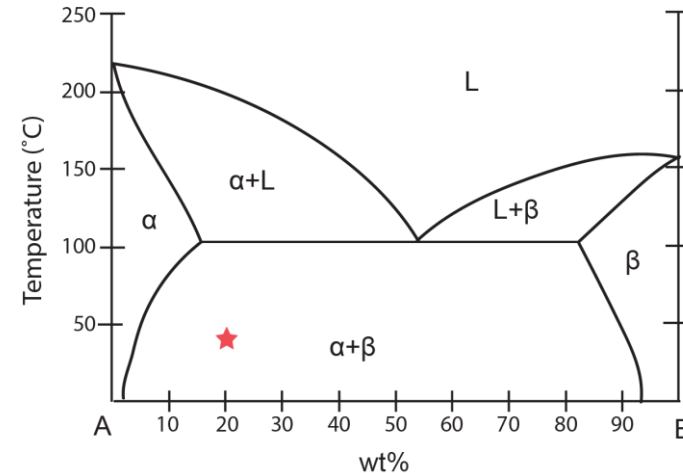
Eutectic, Pro-eutectic phase alpha or beta, etc.

Lever Rule

Used to calculate various phase and microconstituent fractions for two phase regions of binary phase diagrams

$$W_{\beta} = \frac{C_0 - C_{\alpha}}{C_{\beta} - C_{\alpha}}$$

$$W_{\alpha} = \frac{C_0 - C_{\beta}}{C_{\alpha} - C_{\beta}}$$



Information needed:
composition and temperature of interest.
e.g.: 20 wt.% B and 50 °C

Derivation

Assumptions:

- For a two-phase region, the weight fractions must add up to 1

$$W_{\alpha} + W_{\beta} = 1$$

- The mass of component B in both phases must add up to the total amount of B in the alloy

$$W_{\alpha}C_{\alpha} + W_{\beta}C_{\beta} = C_0$$

Derivation

α phase

$$W_{\alpha} + W_{\beta} = 1 \Rightarrow W_{\beta} = 1 - W_{\alpha}$$

$$\Rightarrow W_{\alpha} C_{\alpha} + (1 - W_{\alpha})C_{\beta} = C_0$$

$$\Rightarrow W_{\alpha} C_{\alpha} + C_{\beta} - W_{\alpha}C_{\beta} = C_0$$

$$\Rightarrow W_{\alpha} (C_{\alpha} - C_{\beta}) = C_0 - C_{\beta}$$

$$\Rightarrow W_{\alpha} = \frac{C_0 - C_{\beta}}{C_{\alpha} - C_{\beta}}$$

β phase

$$W_{\alpha} + W_{\beta} = 1 \Rightarrow W_{\alpha} = 1 - W_{\beta}$$

$$(1 - W_{\beta})C_{\alpha} + W_{\beta}C_{\beta} = C_0$$

$$\Rightarrow C_{\alpha} - W_{\beta} C_{\alpha} + W_{\beta}C_{\beta} = C_0$$

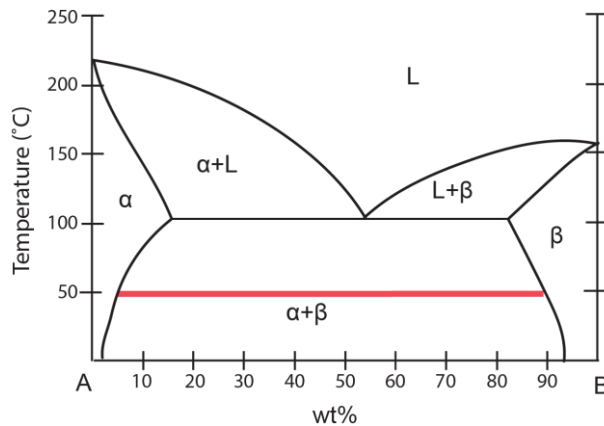
$$\Rightarrow W_{\beta} (C_{\beta} - C_{\alpha}) = C_0 - C_{\alpha}$$

$$\Rightarrow W_{\beta} = \frac{C_0 - C_{\alpha}}{C_{\beta} - C_{\alpha}}$$

Lever Rule Steps

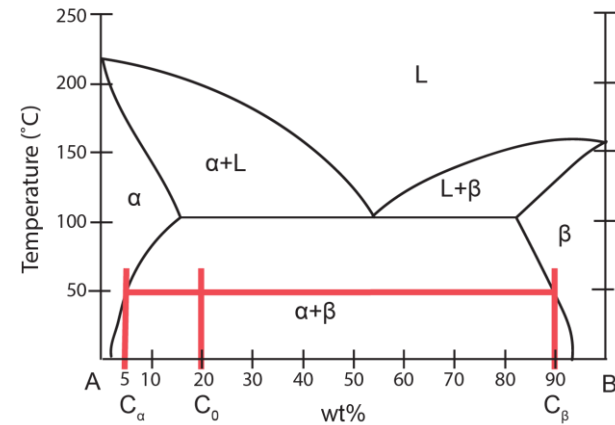
Step 1:

Draw a tie line across the two-phase region



Step 2:

Identify points of interest



Lever Rule Steps

Step 3:

To determine the phase fraction, take the distance from the composition to the *other* phase divided by the total



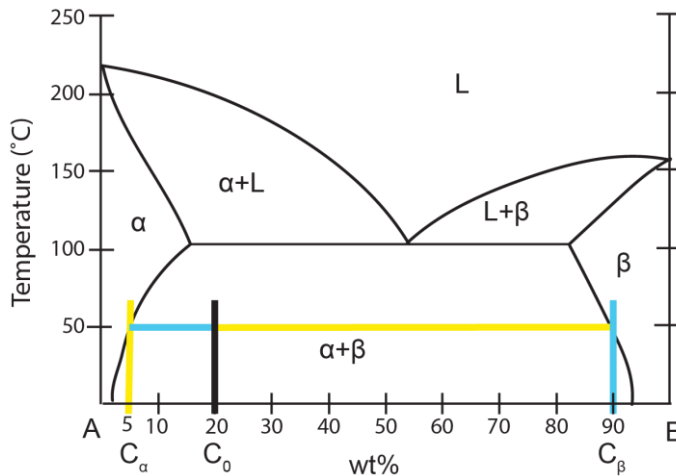
$$W_{\alpha} = \frac{C_0 - C_{\beta}}{C_{\alpha} - C_{\beta}} = \frac{20 - 90}{5 - 90} = \frac{-70}{-85}$$

$$= 0.824 = 82.4 \text{ wt\%}$$

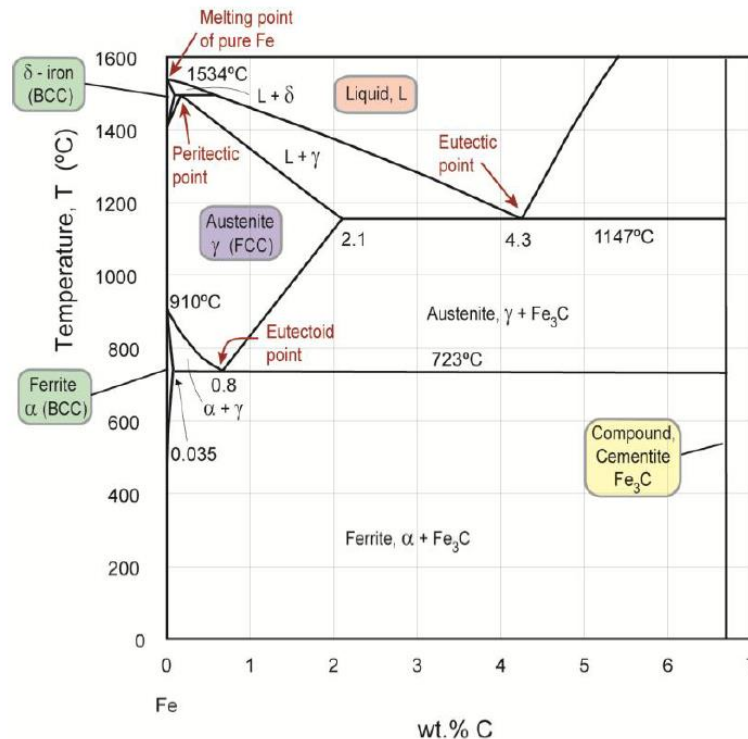


$$W_{\beta} = \frac{C_{\alpha} - C_0}{C_{\alpha} - C_{\beta}} = \frac{5 - 20}{5 - 90} = \frac{-15}{-85}$$

$$= 0.176 = 17.6 \text{ wt\%}$$



The Iron – Carbon phase diagram: EduPack MS&E



Any Questions ???